

# Moving Home: Non-Market Housing and Labour Market Risk

Stephen Hennessy

November 10, 2025

## **New empirical evidence (Health and Retirement Study)**

- ▶ Children who lose their job are more likely to move home with parents
  - ▶ **NEW** Effect is present both at young adulthood and into middle age
  - ▶ Kaplan (2012): evidence for men 17-22, NLSY97
- ▶ Effect is robust to controlling for income, eldercare, and parent characteristics

## **Research questions**

1. How does parental coresidence affect job market search among adult children?
2. How does welfare from coresidence interact with the optimal level of UI?

# Contribution

## **Empirical:** Health and Retirement Study

- ▶ Children are more likely to move home when transitioning into unemployment
  - ▶ **NEW** Observed for children into middle age

## **Quantitative:** structural lifecycle model of job search and coresidence

- ▶ Consumers with the option to move home search in higher-wage submarkets
- ▶ Welfare from the move home option is decreasing in the size of the UI benefit

# HRS Data Selection: Definition of Cross-wave Flows

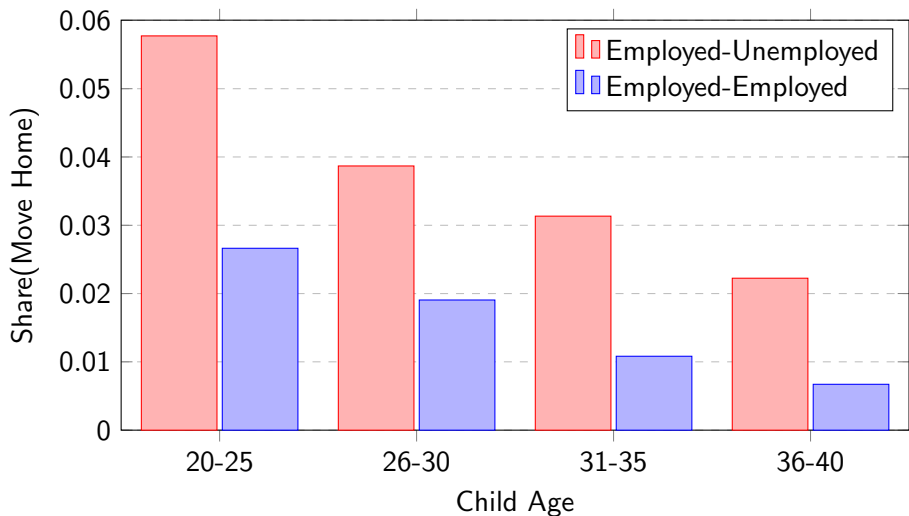
**Employment:** two types of job transitions

1. Employed-Employed: working in two subsequent waves
2. Employed-Unemployed: working in the previous wave but not in the current wave

**Coresidence:** child lives independently previously and coresides in the current wave

- ▶ If parent is a homeowner and child is not: child moves home
- ▶ If child is a homeowner and parent is not: child hosts parent
- ▶ Neither (or both) parent and child are homeowners: ambiguous coresidence

## HRS: E-U children are more likely to move home at all working ages



## Probit: Average Marginal Effects on Share(Move Home)

**Dependent variable:** indicator for moving home after living independently

Independent Variable	Child Age			
	(1) 20-25	(2) 26-30	(3) 31-35	(4) 36-40
Employed-Unemployed	.0312***	.0194***	.0169***	.0050*
Transfer from Parent	.0096*	.0130***	.0078***	.0044***
Child Income				
<10K	<i>Base</i>			
10-35K	-.0173***	-.0036	-.0137***	-.0076**
35-70K	-.0387***	-.0051	-.0245***	-.0147***
70-100K	-.0205	-.0068	-.0268***	-.0154***
100K+	.	-.0039	-.0274***	-.0168***
Child Gender (Female)	.0039	-.0013	-.0074***	-.0048***
Child Marital Status	-.0655***	-.0328***	-.0201***	-.0134***
Child Parental Status	.0162**	-.0050*	.0064***	.0010
<b>Mean Share(MH)</b>	.0301	.0147	.0100	.0071

# Model

## Model – Consumers

- ▶ Consumers are heterogeneous productivity, assets, and age
  - ▶ **NEW** option to coreside with a parent
  - ▶ Assumed to be purely altruistic: no strategic interaction b/t agents
  - ▶ **Tradeoff:** can avoid housing costs but lose out on utility from living independently
  - ▶ Independence utility subject to a Type-I extreme value shock
- ▶ When young, consumers choose:
  - ▶ Submarket (piece-rate) for search
  - ▶ Whether to coreside or live independently (up to age 40)
  - ▶ Saving for next period
- ▶ When old, consumers choose:
  - ▶ Saving for next period



## Consumer Preferences – Utility

$$U(j, a, \epsilon) = \frac{c^{1-\sigma}}{1-\sigma} + d_h \chi$$

Where:

- ▶  $j$ : age
- ▶  $a$ : assets
- ▶  $\epsilon$ : individual-specific productivity
- ▶  $\chi$ : independence utility

$d_h = 1$  when a consumer lives independently,  $= 0$  when they coreside

- ▶ Beyond age 40,  $d_h = 1$  for all consumers

## Consumer Preferences – Budget Constraints

**Employed:**  $c + a' = (1 - \tau)\phi\epsilon_j + (1 + r)a - d_h\kappa_h$

**Unemployed:**  $c + a' = (1 - \tau)b + (1 + r)a - d_h\kappa_h$

**Retired:**  $c + a' = (1 - \tau)S + (1 + r)a - \kappa_h$

Where:

- ▶  $\phi$ : piece-rate determined by submarket choice
- ▶  $b$ : unemployment benefit
- ▶  $S$ : pension benefit
- ▶  $\kappa_h$ : cost of housing
- ▶  $\tau$ : proportional tax on income
- ▶  $r$ : interest rate
- ▶  $a'$ : savings choice

## Labour Market – Workers

- ▶ Directed search in submarkets on age  $j$ , piece-rate  $\phi$ , and worker productivity  $\epsilon$
- ▶ Den Haan matching function  $M(u, v) = \frac{uv}{(u^\alpha + v^\alpha)^{\frac{1}{\alpha}}}$  with market tightness  $\theta = \frac{v}{u}$
- ▶ Find job at rate  $f(\theta) = \frac{M(u, v)}{u}$
- ▶ Provide individual-specific productivity  $\epsilon$  to the firm
- ▶ Earn wage as an after-tax share of output:  $w = (1 - \tau)\phi\epsilon_j$
- ▶ Proportional tax on output finances unemployment benefit  $b$

# Labour Market – Firms

- ▶ Hire worker at rate  $q(\theta) = \frac{M(u,v)}{v}$  after paying posting cost  $\kappa_p$
- ▶ Match is destroyed in each subsequent period with probability  $\delta$

**Firm's value function:**

$$V_f(j, \epsilon, \phi) = \epsilon_j(1 - \phi) + \beta(1 - \delta)V(j + 1, \epsilon, \phi)$$

**Vacancy posting decision:**  $\max\{V_f(j, \epsilon, \phi) - \kappa_p, 0\} \quad \forall j, \epsilon, \phi$

Search Equilibrium

## Value Functions – Young Consumers

$$V_s(j, a, \epsilon) = \max_{\phi} \{ f(\theta(j, a, \epsilon)) V_u(j, a, \epsilon) + [1 - f(\theta(j, a, \epsilon))] V_e(j, a, \epsilon, \phi) \}$$

$$V_u(j, a, \epsilon) = \max \mathbf{E}_{\xi^c, \xi^i} \{ V_u^{cores}(j, a, \epsilon) + \xi^c, V_u^{ind}(j, a, \epsilon) + \xi^i \}$$

$$V_e(j, a, \epsilon, \phi) = \max \mathbf{E}_{\xi^c, \xi^i} \{ V_e^{cores}(j, a, \epsilon, \phi) + \xi^c, V_e^{ind}(j, a, \epsilon, \phi) + \xi^i \}$$

Where:

- ▶  $V_u^{cores}(j, a, \epsilon), V_u^{ind}(j, a, \epsilon)$ : consumer's value of coresiding and living independently while unemployed
- ▶  $V_e^{cores}(j, a, \epsilon, \phi), V_e^{ind}(j, a, \epsilon, \phi)$ : consumer's values while employed
- ▶  $\xi^{cores}, \xi^{ind}$  are Type-I extreme value shocks on the coresidence choice

## Value of Unemployment

$$V_u(j, a, \epsilon) = \max_{\xi_c, \xi_i} \mathbf{E} \{ V_u^{cores}(j, a, \epsilon) + \xi_c, V_u^{ind}(j, a, \epsilon) + \xi_i \}$$

$$V_u^{cores}(j, a, \epsilon) = \max_{a' \geq 0} \left\{ \frac{[b + (1+r)a - a']^{1-\sigma}}{1-\sigma} + \beta V_s(j+1, a', \epsilon) \right\}$$

$$V_u^{indep}(j, a, \epsilon) = \max_{a' \geq 0} \left\{ \frac{[b + (1+r)a - a' - \kappa_h]^{1-\sigma}}{1-\sigma} + \chi + \beta V_s(j+1, a', \epsilon) \right\}$$

## Value of Employment

$$V_e(j, a, \epsilon, \phi) = \max \mathbf{E}_{\xi_c, \xi_i} \{ V_e^{cores}(j, a, \epsilon, \phi) + \xi_c, V_{ind}^e(j, a, \epsilon, \phi) + \xi_i \}$$

$$V_e^{cores}(j, a, \epsilon, \phi) = \max_{a' \geq 0} \left\{ \frac{[(1 - \tau)\epsilon_j \phi + (1 + r)a - a']^{1-\sigma}}{1 - \sigma} + \beta[(1 - \delta)V_e(j + 1, a', \epsilon, \phi) + \delta V^s(j + 1, a', \epsilon)] \right\}$$

$$V_e^{indep}(j, a, \epsilon, \phi) = \max_{a' \geq 0} \left\{ \frac{[(1 - \tau)\epsilon_j \phi + (1 + r)a - a' - \kappa_h]^{1-\sigma}}{1 - \sigma} + \chi + \beta[(1 - \delta)V_e(j + 1, a', \epsilon, \phi) + \delta V_s(j + 1, a', \epsilon)] \right\}$$

## Value Functions – Old Consumers

$$V_r(j, a) = \max_{a'} \left\{ \frac{[S + (1 + r)a - a' - \kappa_h]^{1-\sigma}}{1 - \sigma} + \beta \psi_j V^r(j + 1, a') \right\}$$

Where  $\psi_j$  is a survival probability that increases in age



# Government

The government provides an unemployment benefit ( $b$ ) and pension benefit ( $S$ ) by choosing income taxes ( $\tau$ ) such that:

$$\int \tau \epsilon_j \phi d\omega_e(j, a, \epsilon, \phi) = \int b d\omega_u(j, a, \epsilon) + \int S d\omega_r(j, a)$$

Where  $\omega_e, \omega_u, \omega_r$  are stationary distributions of employed, searchers, and retirees

# Equilibrium

Given initial distributions of assets and productivity there is an equilibrium such that:

1. Consumers solve their problem by choosing a piece-rate, coresidence, and saving
2. Firms face zero expected profits for each submarket in which they post
3. Government funds unemployment and pension benefits via a proportional tax

Solution Algorithm

# Results

## Calibration: Internal

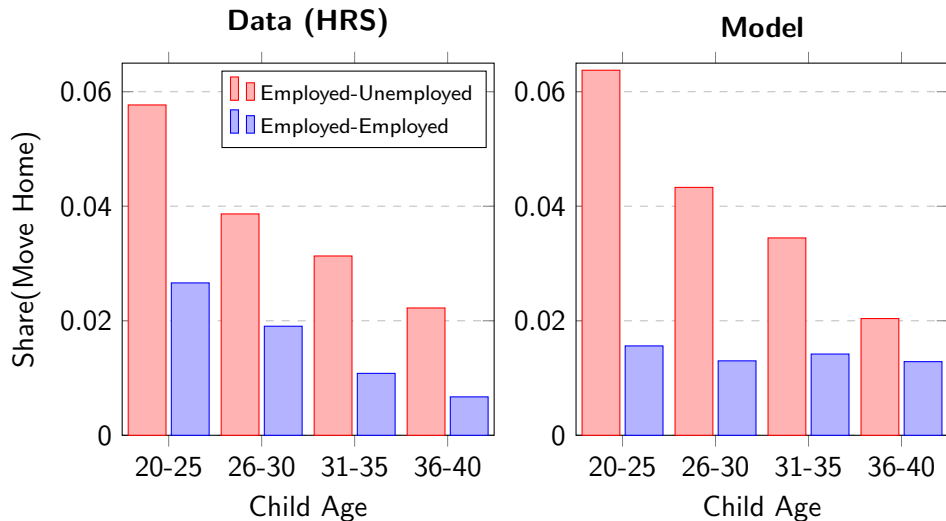
	Parameter	Value	Target	Model	Data
$\kappa_h$	Cost of Housing	.1171	Rent-to-Income Ratio	.0500	
$\chi$	Independence Utility	4.703	E-U Move Home Share	.0413	.0413
$\eta$	EV Distribution Scale	1.000	Coresidence Share	.0273	.1460
$\kappa_j$	Cost of Posting	.0034	Unemployment Share <sup>1</sup>	.0478	.0420
$b$	UI Benefit	.2454	UI Exp. to Income Ratio <sup>2</sup>	.0042	.0042
$S$	Social Security Benefit	.7537	SS Exp. to Income Ratio <sup>3</sup>	.0525	.0525
$\sigma_\epsilon$	St. Dev. Productivity	.8868	SD Log Earnings (Age 26-30) <sup>4</sup>	.9000	.9000

<sup>1</sup> BLS (2025) <sup>2,3</sup> BEA (2024) <sup>4</sup> Kuhn & Ríos-Rull (2013)

## Calibration: External

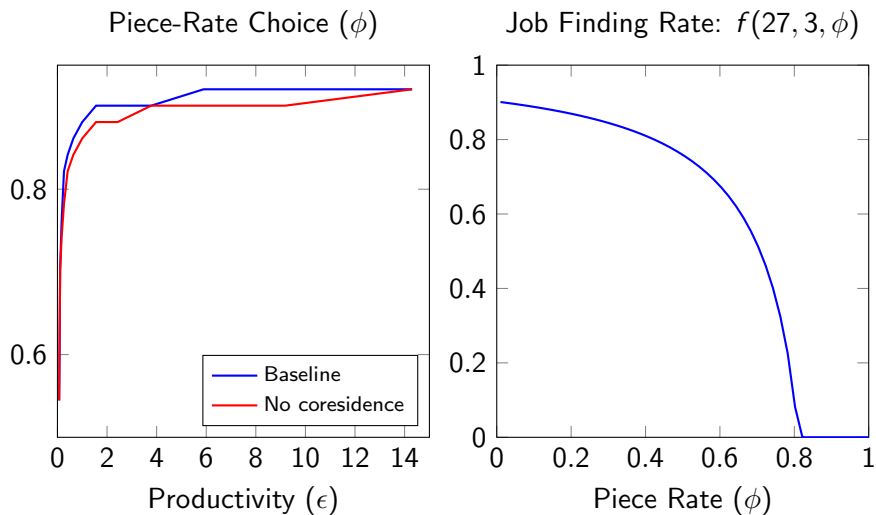
	<b>Parameter</b>	<b>Value</b>	<b>Source</b>
$\alpha$	Match Elasticity	1.27	Den Haan (2000)
$\delta$	Job Destruction Rate	0.0192	E-U Share (HRS)
$\sigma$	Risk Aversion	2	
$\beta$	Discount Factor	0.96	
$r$	Interest Rate	0.04	

## Model Validation: Share who Move Home



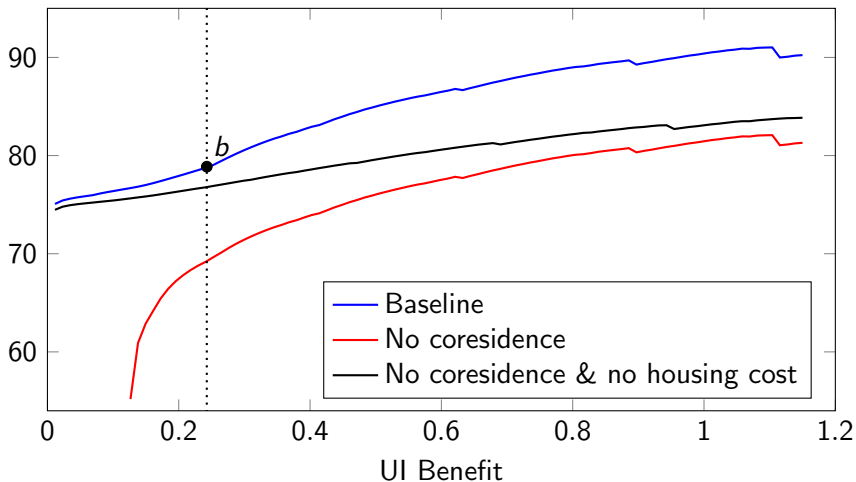
- Move home flows are larger for E-U consumers and are decreasing in age

## Ex Ante Search Choice ( $j = 27, a = .16$ )



- Consumers without the coresidence option search in lower piece-rate submarkets

## Optimal UI Benefit: Expected Lifetime Utility

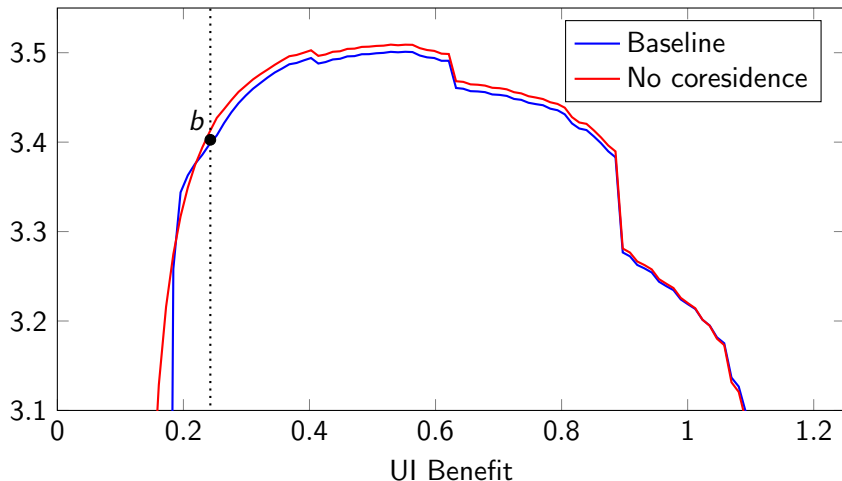


- Consumers prefer higher UI benefits until everyone selects into unemployment

Tax Rate



## Optimal UI Benefit: Equilibrium Utility



- Optimal UI under this welfare measure is roughly twice its calibrated value ( $b$ )

# Conclusion

**Empirical observation:** E-U children are more likely to enter coresidence

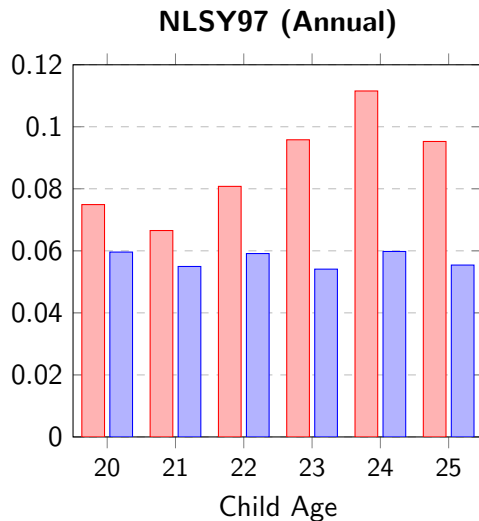
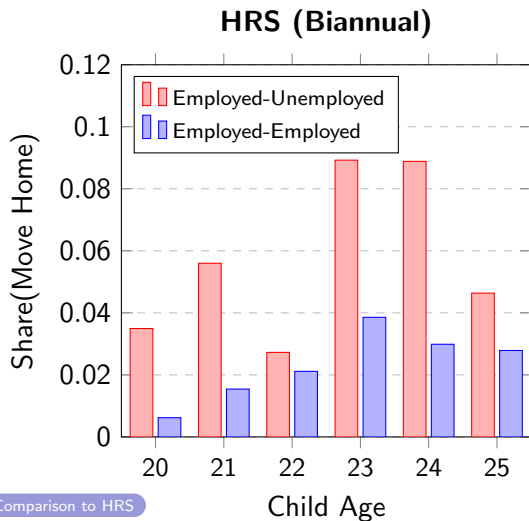
**Structural model:**

1. Children who can coreside search in submarkets with lower job-finding rates
  - ▶ Relative cost of unemployment is lower due to the coresidence option
  - ▶ Coresidence allows children to avoid housing cost  $\kappa_h$
2. Welfare benefits of coresidence are largest at lower unemployment benefits
  - ▶ Suggests coresidence and UI are complementary insurance mechanisms

# Thank you

hennesss@mcmaster.ca  
stephen-hennessy.github.io

## HRS v. NLSY97: E-U young adults are more likely to move home



[Comparison to HRS](#)

[Back](#)

# HRS v. NLSY97

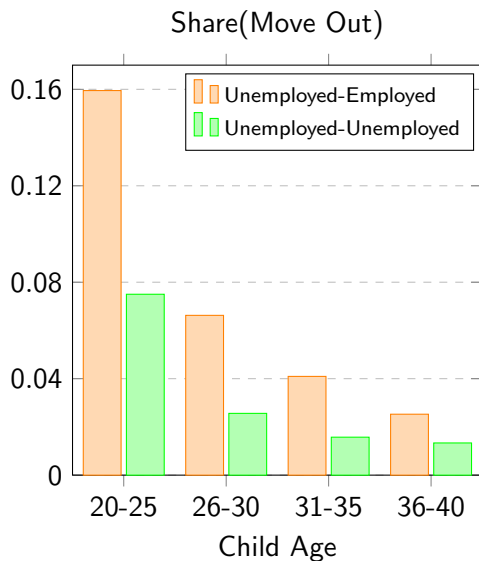
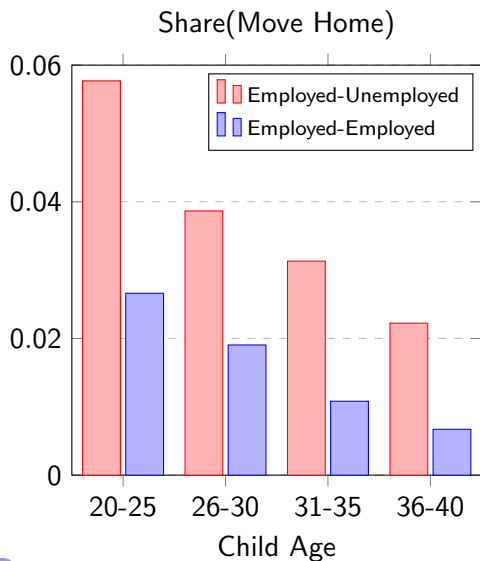
Health and Retirement Study (1998-2018):

- ▶ Biannual frequency, ages 18-45
- ▶ Categorical child income, no unemployment benefits
- ▶ **Coresidence and transfers in all years**

NLSY97 (1998-2021):

- ▶ Annual frequency, ages 18-42
- ▶ Child income, employment, and unemployment benefits
- ▶ **Key variables:**
  1. Coresidence: available until 2009 (age 26)
  2. Transfers: available until 2002 (22); extensive margin until 2011 (age 32)

## Counterfactual: U-E children are more likely to move out



## HRS: Coresidence

- ▶ 8% of adult children (excluding students) live with their parents
- ▶ In any individual wave, 1.3% of adult children move home
  - ▶ 0.71% move in with parents
  - ▶ 0.15% host parents
  - ▶ 0.44% are ambiguous
- ▶ Children who move home tend to be younger and have less education
- ▶ Parents of children who move home have lower incomes but higher wealth

	Move home	Stay independent
Child age	36.2	42.1
Child education (years)	12.4	13.8
Parent income	\$89,357	\$79,104
Parent assets	\$465,707	\$578,635

## HRS: Transfers

Parents transfer choices and co-residence depend on child employment outcomes

- ▶ Children who have recently lost their jobs are more likely to receive transfers relative to those who stay employed
- ▶ The quantity of these transfers is also larger in both the unconditional average and intensive margin
- ▶ Job-losing children are also approximately 3.5 times more likely to move home

	E-U	E-E
Extensive margin	0.1932	0.1672
Intensive margin	\$10,336	\$9,740
Average transfer	\$1,997	\$1,628
Share(Move home)	0.03773	0.01354
Share(MH & Transfer)	0.00683	0.00214



## Linear Probability Model: Share(Move Home)

**Dependent variable:** indicator for moving home after living independently

Independent Variable	Child Age			
	(1) 20-25	(2) 26-30	(3) 31-35	(4) 36-40
Employed-Unemployed	.0315***	.0202***	.0205***	.00814**
Transfer from Parent	.0091*	.0144***	.0092***	.0045**
Child Income				
<10K	Base			
10-35K	-.0186***	-.0056	-.0206***	-.0208**
35-70K	-.0354***	-.0054	-.0313***	-.0284***
70-100K	-.0226	-.0067	-.0321***	-.0286***
100K+	-.0541***	-.0061	-.0334***	-.0282***
Child Gender (Female)	.0046	-.0018	-.0068***	-.0058***
Child Marital Status	-.0418***	-.0312***	-.0235***	-.0174***
Child Parental Status	.0118	-.0044*	.0075***	.0037*
Mean Share(MH)	.0301	.0147	.0100	.0071

\*\*\* 99%, \*\* 95%, \* 90%

## Search Equilibrium

Value for a firm with a match:

$$V_f(j, \epsilon, \phi) = \epsilon(1 - \phi) + \beta(1 - \delta)V_f(j + 1, \epsilon, \phi)$$

Free entry condition:

$$q(\theta(j, \epsilon, \phi))V_f(j, \epsilon, \phi) = \kappa_p \quad \forall j, \epsilon, \phi$$

If  $V_f(j, \epsilon, \phi) < \kappa_j \rightarrow \theta = 0$  since the firm does not post in submarket  $(j, \epsilon, \phi)$

Otherwise:

$$q(\theta) = \frac{\kappa_p}{V_f} = \frac{M(u, v)}{v} = \frac{u}{(u^\alpha + v^\alpha)^{\frac{1}{\alpha}}}$$

$$u = \frac{\kappa_p}{V_f}(u^\alpha + v^\alpha)^{\frac{1}{\alpha}} \Rightarrow \frac{u^\alpha}{u^\alpha + v^\alpha} = \left(\frac{\kappa_p}{V_f}\right)^\alpha$$

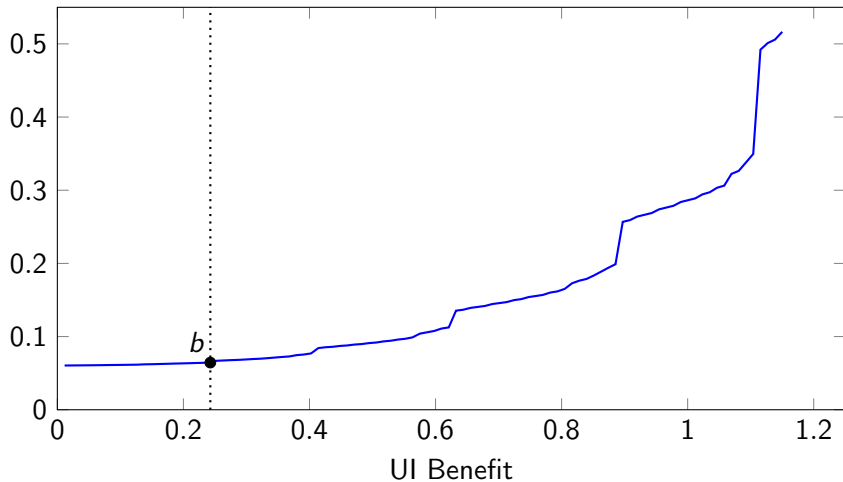
$$1 + \theta^\alpha = \left(\frac{V_f}{\kappa_p}\right)^\alpha \Rightarrow \theta^\alpha = \left(\frac{V_f}{\kappa_p}\right)^\alpha - 1 \Rightarrow \theta = \left[\left(\frac{V_f}{\kappa_p}\right)^\alpha - 1\right]^{\frac{1}{\alpha}} \quad \forall j, \epsilon, \phi$$

# Solution Algorithm

Assuming an initial distribution of consumers ( $\omega_s$ ) at  $j = 1 \forall a, \epsilon$

- (1) Guess labour income tax rate  $\tau \in \{0, 1\}$
- (2) Firm: solve for  $V_f(j, \epsilon, \phi)$  where  $V_f(J, \epsilon, \phi) = 0 \forall \epsilon, \phi$ 
  - ▶ Using  $V_f(j, \epsilon, \phi)$ , compute market tightness  $\theta$
- (3) Consumer: using  $V^r(J, a) = 0 \forall a$ , compute
  - ▶  $V_r(j, a) \forall a$  and  $j \in \{65, \dots, J - 1\}$
  - ▶  $V_u(j, a, \epsilon)$ ,  $V_u^{indep}(j, a, \epsilon)$ , and  $V_u^{cores}(j, a, \epsilon) \forall a, \epsilon$  and  $j \in \{0, \dots, 64\}$
  - ▶  $V_e(j, a, \epsilon, \phi)$ ,  $V_e^{indep}(j, a, \epsilon, \phi)$ , and  $V_e^{cores}(j, a, \epsilon, \phi) \forall a, \epsilon, \phi$  and  $j \in \{0, \dots, 64\}$
  - ▶  $V_s(j, a, \epsilon) \forall a, \epsilon$  and  $j \in \{0, \dots, 64\}$
- (4) Compute distributions for workers  $\omega_s(j, a, \epsilon)$ ,  $\omega_e(j, a, \epsilon, \phi)$  and retirees  $\omega_r(j, a)$
- (5) Compute tax rate to balance the government's budget constraint; update guess
- (6) Iterate on (2) – (5) until convergence

## Tax Rate: Expected Lifetime Utility



## Tax Rate: Equilibrium Utility

